

MIDTERM EXAMINATION (In Class; Closed Book)  
12 MAY  
(100 POINTS)

1) (20 points) A one-dimensional harmonic oscillator is subjected to a perturbation of the type  $ax^3$ . Use stationary perturbation theory through second order to determine the correction to the ground state energy.

$$E_n = \hbar\omega(n + 1/2); \quad \langle x \rangle_{n, n+1} = \left\{ \frac{\hbar(n+1)}{2\mu\omega} \right\}^{1/2}$$

2) (40 points) Find the best value for the ground state energy for a particle of mass  $m$  in the gravitational potential:

$$V = gz; \quad z \geq 0; \quad V = 0; \quad z < 0$$

with the variational trial function  $\psi = \exp(-az)$ . Then compare your answer with that obtained from the WKB approach.

3) (40 points)

- a) (12 pts) A hydrogen atom in its 1s state is placed in a static electric field directed along the z-axis for a time  $t$ . Use time-dependent perturbation theory (first order) to determine the probability of transition to the  $2p_0$  level as a function of  $t$ .  $\langle 2p_0 | ez | 1s \rangle = 0.74ea_0$ .  $E_n = -e^2 / 2a_0n^2$
- b) (12 pts) How does your answer to a) change if instead of a static field, monochromatic radiation of resonant frequency  $\omega$  is used?
- c) (16 pts) How does your answer to b) change if instead of monochromatic radiation, a range of frequencies centered on the resonant frequency is used?

Do not use the infinite time limit. For part (c), assume a flat distribution function  $g(\omega)$  and integrate over all frequencies.