

Physics 517/617 Homework 5 (Due Nov. 3rd)

Problem 1. (Note: Maple (expand and contract) or Mathematica make plotting and solving this problem simple)

The following problem is designed to familiarize you with the concept of amplitude modulation. This concept is obviously crucial to the understanding of the AM radio you are about to build. The general expression for an Amplitude Modulated voltage is:

$$V = (1 + a \cos(\omega_m t)) \cos(\omega_c t)$$

In this expression ω_c is the carrier frequency, ω_m is the modulating frequency and a is the amount of modulation ($0 < a < 1$). For the AM radio example the carrier frequency, ω_c , is high frequency (hundreds of kHz) while the modulating, ω_m , frequency is low frequency (audio frequency 20Hz to 20 KHz).

- 1) Make a sketch of V vs t if one assumes $\omega_m = 1$ KHz, $\omega_c = 10$ KHz, and $a=1$.
- 2) Show that V can be written in the following form which contains three frequencies. Relate ω_1 , ω_2 , and ω_3 to ω_m and ω_c :

$$V = \cos(\omega_1 t) + \frac{1}{2} \cos(\omega_2 t) + \frac{1}{2} \cos(\omega_3 t)$$

- 3) A Taylor Expansion for small voltages (V) of the Ebers-Moll (or Diode) equation for current (I) has the following form:

$$I = \alpha V + \beta V^2$$

where α and β are constants. Assuming that the current is given by this expression and the voltage is given by the expression in part 2. Show that the resulting current has a term that depends linearly on $\cos \omega_m t$ and a term that depends linearly on $\cos \omega_c t$ (it also has many other terms).

- 4) Use the results of part 3 to describe how a high frequency AM signal gets demodulated (turned into audio frequencies) in the radio you will be building in lab. Which frequencies are amplified and which are filtered out ?

Problem 2: The transistor has parameters $\beta = h_{fe} = 100$, $h_{ie} = 2k\Omega$, and $h_{oe} = 0\Omega^{-1}$.

Calculate a) the input resistance R_i , and b) the amplifier voltage gain $G = \frac{v_C}{v_i}$.

(You may assume the impedance of the capacitors is negligible at signal frequencies.)

