

# Embedded-Atom Method Potential for Niobium

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## Motivation

- Simulation of complex processes in metallic alloys (e.g., Ti-Nb~Gum Metal)
  - plastic deformation
  - phase transformations
- Require large systems (thousands to millions of atoms)
  - first-principles calculations are too expensive ( $t_{\text{sim}} \sim N^3$ )
  - classical interatomic potentials allow large-scale simulations ( $t_{\text{sim}} \sim N$ )

## Embedded-Atom Method (EAM) Potentials<sup>1</sup>

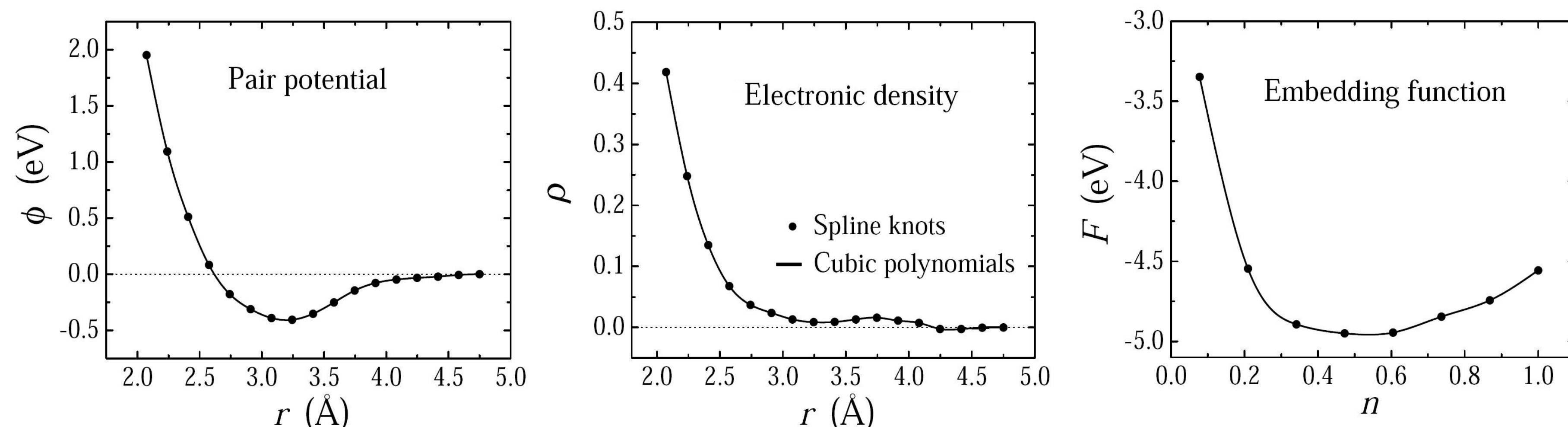
- EAM energy of a collection of atoms:

$$E = \sum_{i>j} \phi(r_{ij}) + \sum_i F(n_i) \quad n_i = \sum_{j \neq i} \rho(r_{ij})$$

- $\phi$  is the pair-potential between atoms  $i$  and  $j$
- $\rho$  is the electronic density associated with a given atom
- $F$  is the *embedding energy* associated with embedding atom  $i$  in the local electronic density  $n_i$
- $F$  is non-linear and implicitly contains many-body effects

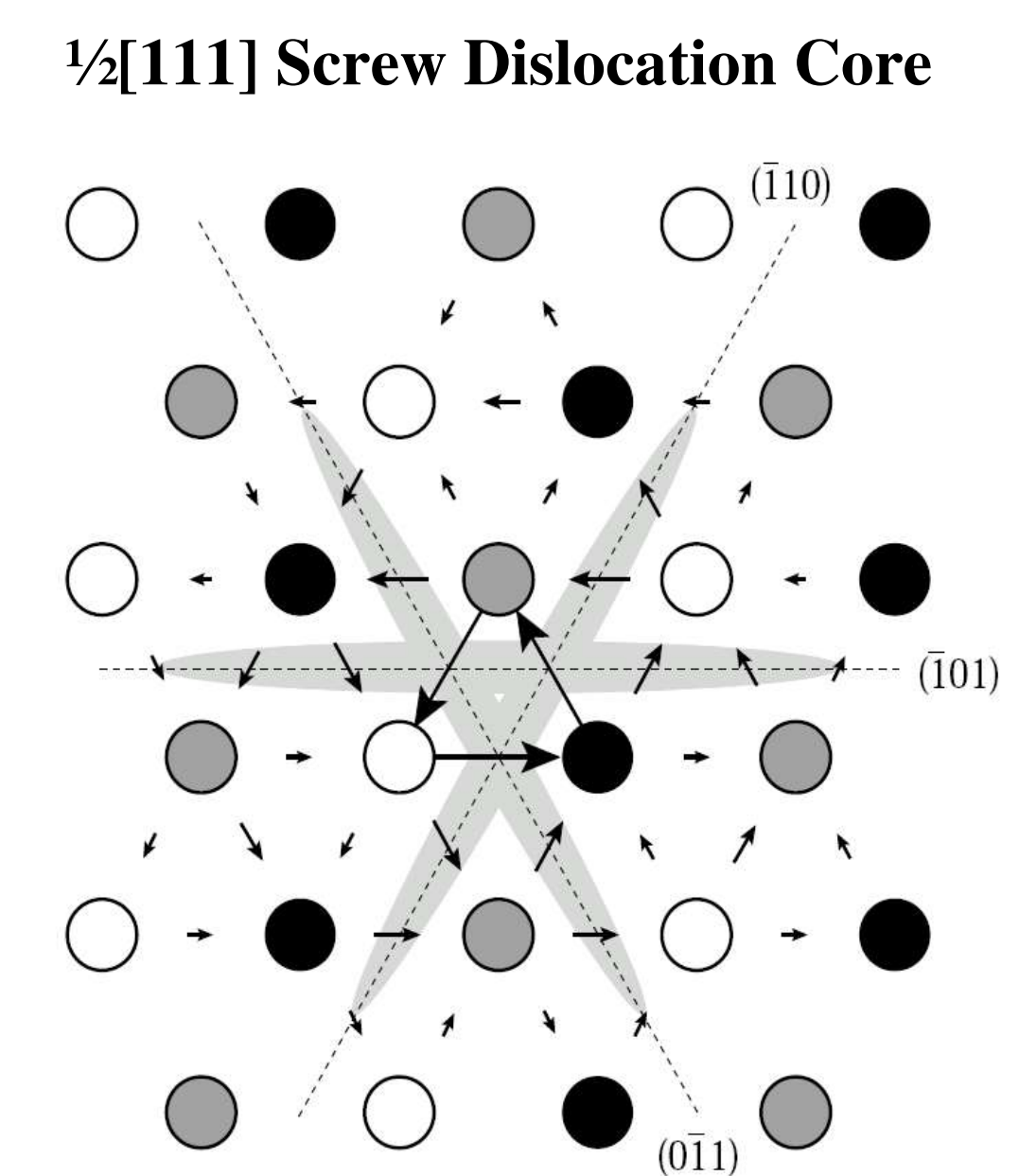
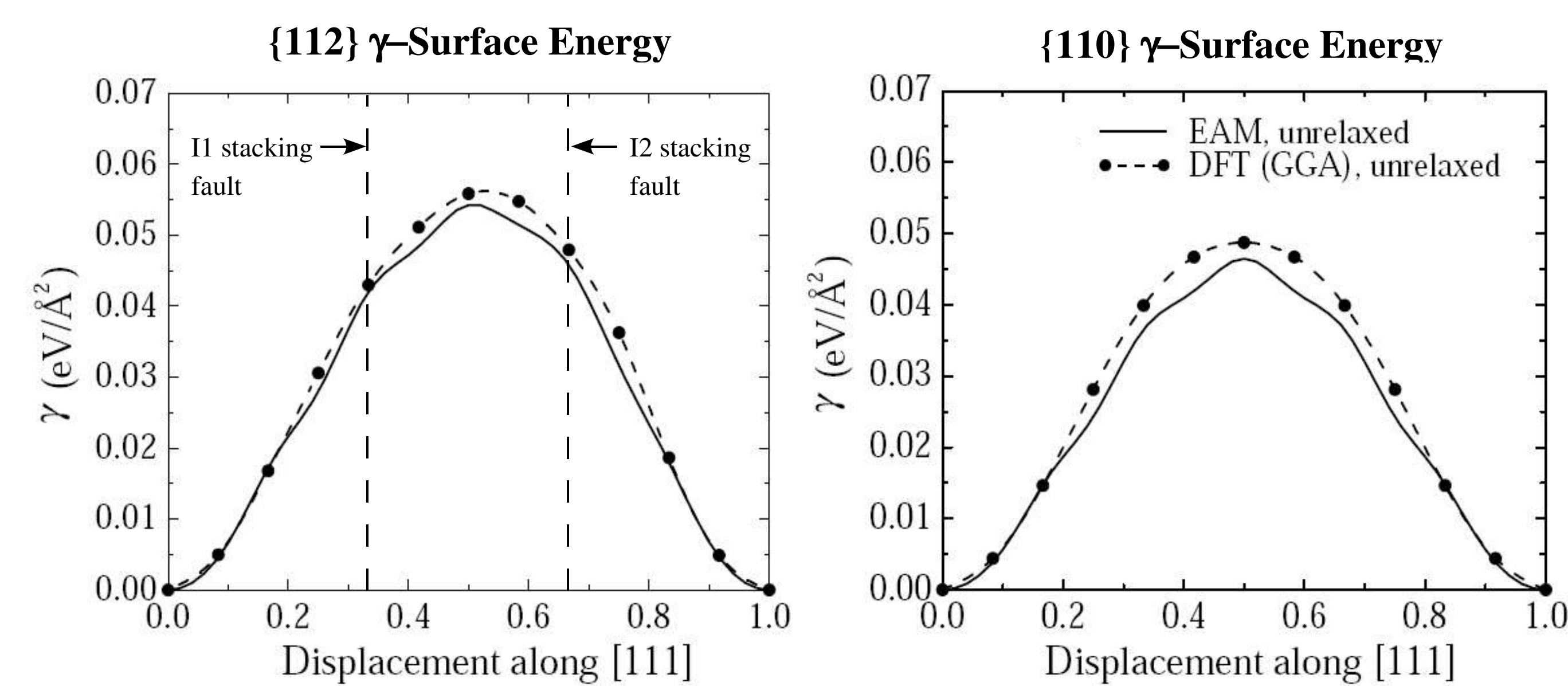
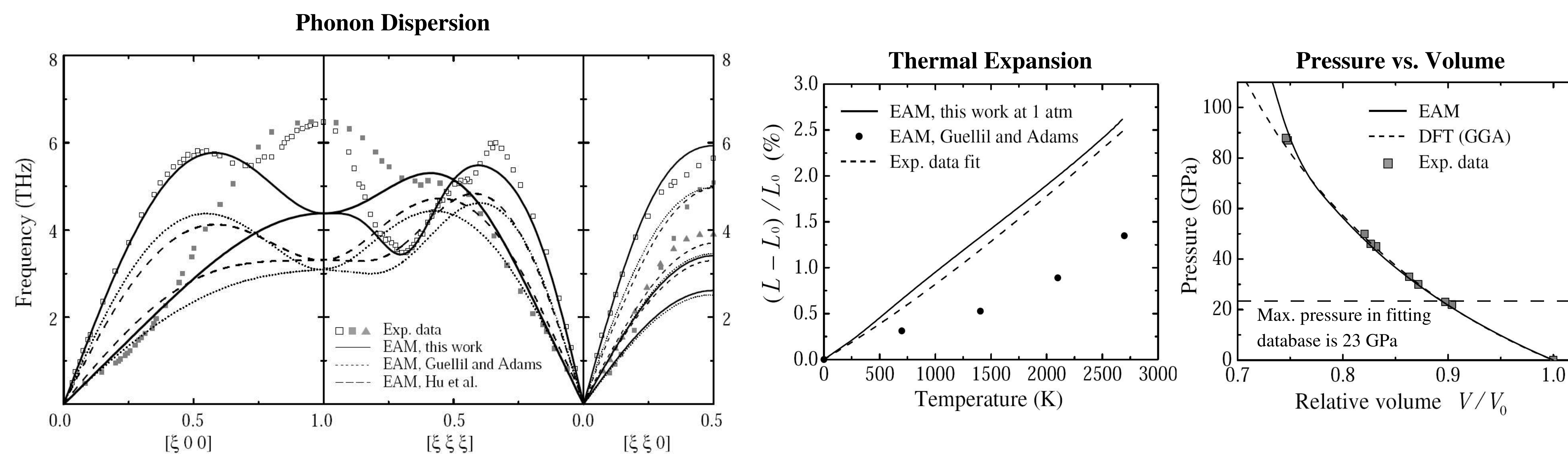
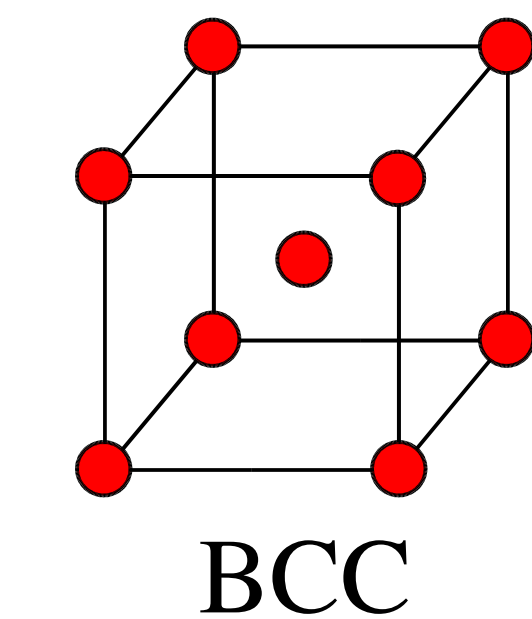
## Optimization Procedure

- The force-matching method<sup>2</sup> is used to construct the potential:
  - Accurate **forces** yield realistic **dynamics**
  - $\phi$ ,  $\rho$ , and  $F$  are represented as cubic splines
  - The code *potfit*<sup>3</sup> optimizes the spline knots to reproduce a large database of density-functional theory **forces**, **energies**, and **stresses** (no experimental data)
  - The fitting database contains snapshots from first-principles MD simulations of structures under various temperature and strain conditions
  - Optimized EAM functions:



## Results for BCC Niobium

	EAM	DFT (GGA)	Experiment
$a$ (Å)	3.308	3.309	3.303
$E_{\text{coh}}$ (eV)	7.09	7.10	7.57
$B$ (GPa)	172	170	173
$C_{11}$ (GPa)	244	246	253
$C_{12}$ (GPa)	136	132	133
$C_{44}$ (GPa)	32	19	31
$Q_{\text{vac}}$ (eV)	3.87	...	3.88(0.3)
$E_{\text{surf}}^{100}$ (eV/Å <sup>2</sup> )	0.147	0.146	Polycrystalline value:
$E_{\text{surf}}^{110}$ (eV/Å <sup>2</sup> )	0.127	0.131	0.14 - 0.17
$E_{\text{surf}}^{111}$ (eV/Å <sup>2</sup> )	0.154	0.149	
$T_{\text{melt}}$ (K)	2685	...	2742



- The EAM potential accurately describes the properties of niobium, even though no surfaces, stacking faults, dislocations, or highly compressed structures are included in the fitting database!

[1] M. S. Daw and M. I. Baskes, *Phys. Rev. Lett.* **50**, 1285 (1984). [2] F. Ercolessi and J. B. Adams, *Europhys. Lett.* **23**, 583 (1994). [3] P. Brommer and F. Gähler, *Modelling Simul. Mater. Sci. Eng.* **15**, 295 (2007).