

## Period 1 Activity Sheet Solutions: Intro to the World of Energy

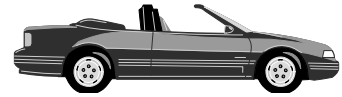
### 1.1 What Are Ratios? How Are They Used?

Your instructor will introduce the concepts of ratios and "per." Use this information to answer the questions in this section.

- a) Ratios are useful when making comparisons. Use ratios to compare the number of miles each vehicle can travel using one gallon of gas.

- 1) A sports car uses 0.8 gallons of gas to travel 17 miles. How many miles per gallon does it get?

$$\frac{17 \text{ miles}}{0.8 \text{ gal}} = 21 \text{ miles/gal}$$



- 2) A sports utility vehicle uses 3.9 gallons of gas to travel 57 miles. How many miles per gallon does it get?

$$\frac{57 \text{ miles}}{3.9 \text{ gal}} = 15 \text{ miles/gal}$$



- 3) How many gallons of gas does the sports car require to travel 243 miles?

$$243 \text{ miles} \div \frac{21 \text{ miles}}{1 \text{ gal}} = 12 \text{ gal}$$

- b) The next activity illustrates how ratios are used to convert units.

- 1) Using the blue balances on your table, place washers in the center of one balance pan and plastic chips in the center of the other pan.

- a) How many chips are required to balance one washer? 9

- b) Write the number of chips per washer as a ratio.

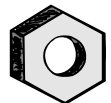
$$\underline{9 \text{ chips/1 washer}}$$

- 2) Using the balance, find how many chips are required to balance one metal nut. Write the number of chips per nut as a ratio.

$$\underline{3 \text{ chips/1 nut}}$$



Washer



Nut

- 3) *Without using the balance*, calculate how many nuts there are per washer. Show the steps in your calculation, including units and how they cancel.

$$\frac{9 \text{ chips}}{1 \text{ washer}} \times \frac{1 \text{ nut}}{3 \text{ chips}} = \frac{9 \text{ nuts}}{3 \text{ washers}} = \frac{3 \text{ nuts}}{1 \text{ washer}}$$

$$\underline{3 \text{ nuts/washer}}$$

- 4) Use the balance to check your answer to part c. How many nuts balance one washer? 3

- c) Use ratios to convert 10 miles/1 gallon of gas into kilometers/liter. Show the steps in the calculation, including units and how they cancel. (Hint: 1 mile = 1.609 kilometers and 1 gallon = 3.785 liters.)

$$\frac{10 \text{ mi}}{1 \text{ gal}} \times \frac{1.609 \text{ km}}{1 \text{ mi}} \times \frac{1 \text{ gal}}{3.785 \text{ l}} = \frac{16.09 \text{ km}}{3.785 \text{ l}} = \frac{4.251 \text{ km}}{1 \text{ liter}}$$

- d) Group Discussion Question: List some common ratios. Why are ratios useful?

## 1.2 How are Ratios Used to Calculate Efficiency?

Your instructor will discuss ratios and the efficiency of energy processes.

- a) Connect one hand-cranked generator to a second hand-cranked generator. Turn the crank of the first generator **slowly** 10 full revolutions.

1) How many revolutions did the crank of the second generator turn?  
\_\_\_\_\_

2) Calculate the efficiency of the system of two generators when the first generator crank is turned slowly.

**If the second generator crank turned 6.5 revolutions, the efficiency =  $6.5/10 = 0.65 = 65\%$**

3) Turn the first generator's crank **rapidly** 10 full revolutions. How many revolutions did the crank of the second generator turn? \_\_\_\_\_ Calculate the efficiency when the first generator crank is turned rapidly.

**The efficiency will be greater when the crank is turned rapidly because the effect of friction in the moving parts of the generator is less.**

4) Why does the efficiency depend on the speed of the cranking? Is it possible to turn the first generator crank 10 revolutions so rapidly that the second crank also turns 10 revolutions? Why or why not?

**Turning the crank more rapidly reduces the friction in the gears of the crank. However, it is not possible to turn the first crank so fast that friction is eliminated. The system of two cranks is never 100% efficient.**

- b) Watch the demonstration of an exercise bicycle connected to light bulbs. The energy used to pedal the bicycle and to light the bulbs is measured in units of joules.

1) Each lit bulb requires 50 joules of energy per second. What is the total energy per second required to light all of the bulbs in this demonstration?  
**250 J/s**

2) If the person pedaling the bicycle expends 1,300 joules of energy per second, what is the efficiency of the bicycle and light system when all the bulbs are lit?

**$\text{Eff} = \frac{\text{Useful Energy Out}}{\text{Total Energy In}} = \frac{250 \text{ J/s}}{1,300 \text{ J/s}} = 0.19 = 19\%$**

## 1.3 How Do Exponents and Scientific Notation Simplify Calculations?

Your instructor will discuss the meaning of exponents. Use this information to calculate the base 2 raised to an exponential power.

- a) Bill says that  $2^2 \times 2^3 = 2^{2 \times 3}$ . Denise says that  $2^2 \times 2^3 = 2^{2+3}$ . To decide whose method is correct, answer the questions below.

1) How much is  $2^2$ ?  **$2 \times 2 = 4$**   $2^3$ ?  **$2 \times 2 \times 2 = 8$**   $2^2 \times 2^3$ ?  **$4 \times 8 = 32$**

2) How much is  $2^{2 \times 3}$ ?  **$2^6 = 2 \times 2 \times 2 \times 2 \times 2 \times 2 = 64$**

- 3) How much is  $2^{2+3}$ ?  **$2^5 = 2 \times 2 \times 2 \times 2 \times 2 = 32$**
- 4) Based on your calculations, which method is correct? State the rule for multiplying numbers with exponents.

**Adding exponents gives the correct answer. When multiplying numbers with exponents, add the exponents.**

- 5) Apply the rule you found for the base 2 to calculations using the base 10 raised to an exponential power.  
How much is  $10^3 \times 10^6$ ?  **$10^{3+6} = 10^9$**

- b) Sarah says that  $10^6 / 10^2 = 10^{6/2}$ . Jason says that  $10^6 / 10^2 = 10^{6-2}$ . Based on your answer to question 4, predict the rule for dividing numbers with exponents. Then check your rule by using it to answer the questions below.

- 1) How much is  $10^6$ ?  **$1,000,000$**   $10^2$ ?  **$100$**   $10^6 / 10^2$ ?  **$10,000$**
- 2) How much is  $10^{6/2}$ ?  **$10^3 = 1,000$**
- 3) How much is  $10^{6-2}$ ?  **$10^4 = 10,000$**
- 4) State the rule for dividing numbers with exponents.

**When dividing numbers with exponents, subtract the exponents.**

At this point, your instructor will give you information about scientific notation. Scientific notation usually means writing one digit to the left of the decimal times the base 10 raised to an exponential power. For example, in scientific notation  $13,300 = 1.33 \times 10^4$ .

- c) Write each of the quantities below in scientific notation, as an integer, and in words. First find the answer **without** using a calculator. Then check your answer with a calculator.

Example:  $(2 \times 10^2) \times (7 \times 10^4) = (2 \times 7) \times 10^{2+4} = 14 \times 10^6 = 1.4 \times 10^7 = 14,000,000 = 14$  million

- 1)  $(5 \times 10^1) \times (3 \times 10^2) = (5 \times 3) \times 10^{1+2} = 15 \times 10^3 = 1.5 \times 10^4 = 15,000 = 15$  thousand
- 2)  $(7 \times 10^3) \times (1 \times 10^{-3}) = (7 \times 1) \times 10^{3-3} = 7 \times 10^0 = 7 \times 1 = 7$
- 3)  $10^{10} / 10^5 = 10^{10-5} = 10^5 = 100,000 = 1$  hundred thousand
- 4)  $(8 \times 10^6) / (2 \times 10^3) = (8/2) \times 10^{6-3} = 4 \times 10^3 = 4,000 = 4$  thousand
- 5)  $(6 \times 10^3) / (2 \times 10^5) = (6/2) \times 10^{3-5} = 3 \times 10^{-2} = 0.03 = 3$  one hundredths
- 6)  $(9 \times 10^6) / (3 \times 10^{-3}) = (9/3) \times 10^{6-(-3)} = 3 \times 10^9 = 3,000,000,000 = 3$  billion

d) Your instructor will discuss the energy content of some common fuels. Use this information, along with ratios and scientific notation, to make the comparisons below.

1) How many kilograms of wood are needed to produce the same amount of energy as 1 kg of coal?

$$\frac{2.9 \times 10^7 \text{ J/kg of coal}}{1.4 \times 10^7 \text{ J/kg of wood}} = 2.1 \text{ kg of wood/kg of coal}$$

2) How many kilograms of crude oil are needed to produce the same amount of energy as 1 kg of Uranium <sup>235</sup>?

$$\frac{8 \times 10^{13} \text{ J/kg of U}^{235}}{4.3 \times 10^7 \text{ J/kg of oil}} = 1.9 \times 10^6 \text{ kg of oil/kg of U}^{235}$$

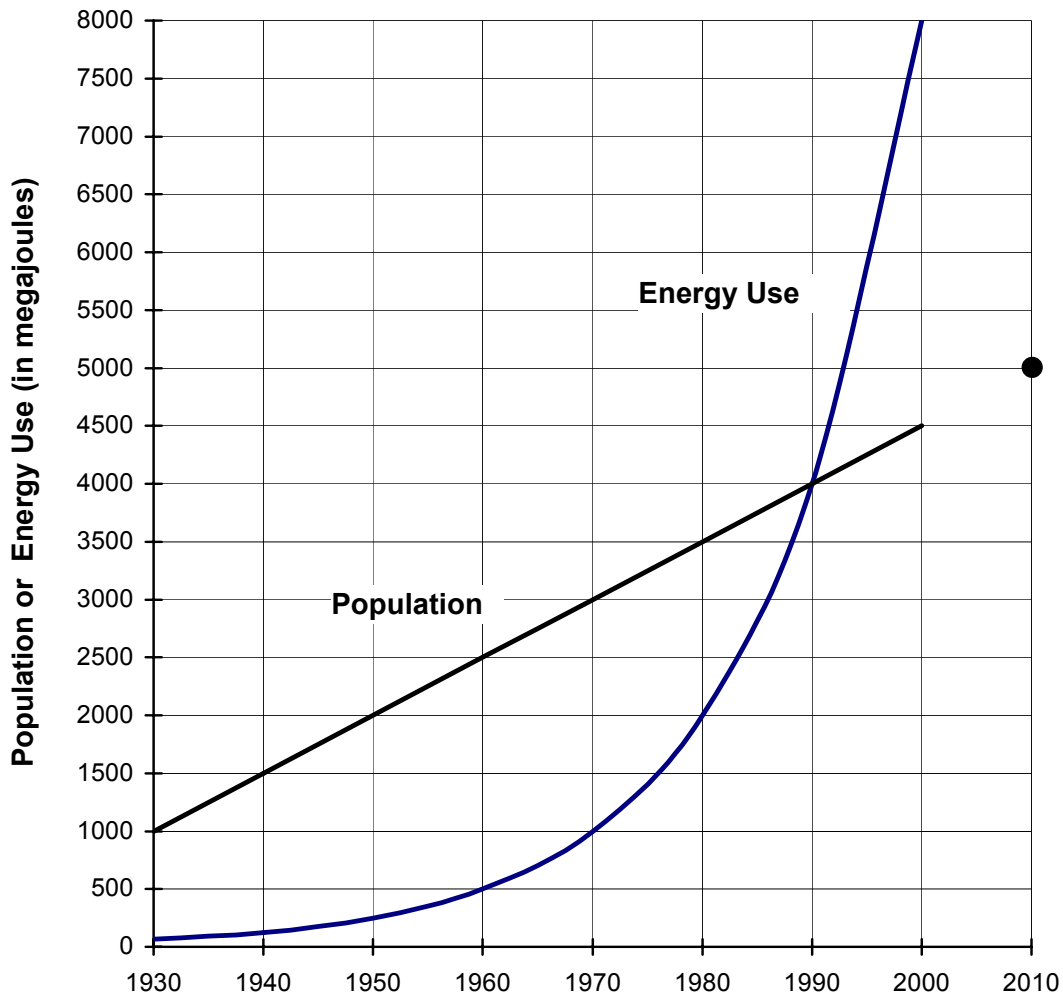
3) An electric generating plant burns coal to produce electricity. If burning 1 kg of coal produces  $1.1 \times 10^7$  joules of energy, what is the efficiency of burning coal to produce electricity?

$$\text{Eff} = \frac{\text{Useful Energy Out}}{\text{Total Energy In}} = \frac{1.1 \times 10^7 \text{ J}}{2.9 \times 10^7 \text{ J}} = 0.38 = 38\%$$

#### 1.4 What is the Difference between Linear and Exponential Growth?

Your instructor will discuss linear and exponential growth using the graph on the next page.

**Fig. 1 Sample Data on Energy Use and Population**



- Find the rate of increase (the slope) of the linear graph. **\_50 people/yr\_**
- If this growth rate remains constant after the year 2000, what will the population be in 2010? **\_5,000\_** Add a data point to the graph to show the population in 2010.
- Starting with 1970**, find the doubling time of the exponential graph. **\_10 years\_**
- If energy use continues to increase at the same rate, what will the energy use be in 2010? **\_16,000 MJ\_** Where would a data point for energy use in 2010 be located?  
**Above the top of the page.**
- Using the doubling time from part c), calculate the energy use in 1930. **\_62.5 MJ\_**
- Group Discussion Question: If someone gave you \$1 and offered to double every day the amount you have, how much would you have on day 7? **\_ $\$1 \times 2^6 = \$64$ \_**  
How much would you have on day 30? **\_ $\$1 \times 2^{29} = \$ 536,870,912$ \_**